



Effizienzaspekte von Information Retrieval

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This talk includes material from

- Andreas Broschart
- Debapriyo Majumdar
- Martin Theobald
- Gerhard Weikum

• and myself ;-)



Outline

- Efficient Centralized Query Processing
 - Introduction
 - Basic Top-k Algorithms
 - Scheduling 1x1
 - Approximation Algorithms
 - Non-Traditional Top-K Processing
- Efficient Precomputation
 - The Map-Reduce Framework
- Efficient Distributed Query Processing



Part 1 – Efficient <u>Query</u> Processing

General Data Model:

- Set of data items D ("documents")
- Set of attributes T ("terms")
- Each item d:
 - Set of attribute values s_t(d) for all t∈T ("term frequencies", "scores")
 - Importance weight w(d) ("page rank")

Any implementations of values and weights suitable that satisfy $0 \le s_t(d) \le 1$ and $0 \le w(d) \le MAX_WEIGHT$



(Simple) Query Model

Input: query q={t1...tn} on D "efficient query processing" on the Web Output: subset R \subseteq D of items where F(s_{t1}(d),...,s_{tn}(d)) $\geq \theta$ "score of d for q" for some (monotonous) function F and some threshold θ

More fancy query models: Term weights, mandatory terms, negative terms, phrases



Common Instances of this Model

- Boolean (unranked) queries and scores:
 s_t(d)=1 iff d contains t, 0 else
 - conjunctive Boolean: "efficient and effective"
 F(x1...xn)=x1·...·xn=min(x1...xn)
 - disjunctive Boolean: "efficient or effective"
 F(x1...xn)=x1+...+xn or F(x1...xn)=max(x1...xn)
 - Threshold θ =1 in both cases



Common Instances of this Model

- Ranked queries:
 - s_t(d) ~ importance of t in d,
 importance of t in D,
 features of D (like length), ...

tf*idf, BM25 Okapi

- most frequent implementation of F:
 F(x1...xn)=x1+...+xn (summation)
- Threshold θ = score of kth result in score order

Focus of part 1:

"Find the k results with highest aggregated score"



Part 1 – <u>Efficient</u> Query Processing

Different aspects of efficiency:

- 1. user-oriented: minimize query answer time
- **2. system-oriented**: maximize query throughput
- **3. resource-oriented**: minimize disk accesses, memory footprint, CPU cycles, energy consumption, ...

Difficult to optimize 1+2 together; combine goals: Maximize throughput such that query answer time is below 0.1s for 95% of queries



Part 1 – <u>Efficient</u> Query Processing

Different aspects of efficiency:

- 1. user-oriented: minimize query answer time
- **2. system-oriented**: maximize query throughput
- **3. resource-oriented**: minimize disk accesses, memory footprint, CPU cycles, energy consumption, ...

Focus of part 1:

Resource-oriented optimization to reduce answer time



Part 1 – Efficient Query Processing

Fundamental data structure: Inverted List

- Inverted List L(t) for a term t consists of sequence of tuples (d,payload)
- each d contains term t
- payload is additional information
 - $-s_t(d)$
 - frequency of t in d
 - positions of t in d (for phrases)

Order of tuples depends on processing strategy



Inverted Lists

 Implementation usually as compressed file with all inverted lists for a collection plus access index



 Alternative implementation (simpler, but slower): use big database table with index on t (plus additional columns, depending on sort order)

t d score(d,t)



Index Compression

Why?

- Smaller index, may fit in memory
- Faster list access when stored on disk

Comes with two kinds of execution cost:

- Compression effort at indexing time
- Decompression effort at query time

Important to keep this low



Compression/Performance Tradeoff

When does it pay off to compress?







Common method: \Delta encoding & vbytes



naive: 2x4 bytes per posting 0 101 1 186 Ω

#bytes per field: 2+1 bytes



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Three main Classes of Algorithms

- Term-at-a-time (TAAT)
- Document-at-a-time (DAAT)
- Score-at-a-time (SAAT)



Term-at-a-Time Processing

- Lists sorted by d (technically, by d's unique ID)
- Lists read one after the other
- Partial scores of results maintained
- Implemented by 2-way merge join with skipping
- Results sorted by score to get top-k results

		Pros:	
increasing ID	D1: 0.15	 Independent of payload 	
	D2: 0.51	 Best for Boolean queries 	
	D3: 0.01	Cons:	
	D4: 0.77	 Needs to load and consider complete lists 	
	D8: 0.99	Requires D intermediate variables	
		 Requires sorting (D ·log D time) 	

[Anh et al., CIKM 06]

Conjunctive Term-at-a-time Processing



RSet 3

D1: 0.51

Even more skipping with block-structured lists:



Layered (or Impact-Ordered) Indexes

List 1 4 Layers of List 1 4 Layers of List 2 max=31.7 max=25.3



Current top-k results + candidates

disjunctive query with both lists



same idea as [Bast et al, VLDB 06]



Document-at-a-Time Processing

- Lists sorted by d (technically, by d's unique ID)
- joined by n-way merge join
- Top-k results computed on the fly





Efficient DAAT: WAND



current top-1

d**doq42: 25.**6

Sort lists in ascending order of current doccid

[Broder et al., CIKM 03]



Efficient DAAT: WAND



[Broder et al., CIKM 03]



Efficient DAAT: WAND



Score this document, replace top-1 if possible, resort lists, ...

current top-1

doc 42: 26.6

Improvement:

consider per-list blocks & per-block max score [Ding&Suel, SIGIR 11]



[Broder et al., CIKM 03]

Score-at-a-Time Processing

Goal:

Avoid reading of complete lists (millions of entries)

Observation:

"Good" results have high scores

- \Rightarrow Order lists by descending scores
- \Rightarrow Have "intelligent" algorithm with early stopping



List Access Modes

Factors of disk access cost:

Seek time, rotational delay, transfer time

- Sequential (sorted)
 - Access tuples in list order
 - Seek time & rotational delay amortized over many accesses

Random

- Look up list entry for specific item
- Pay full cost (plus lookup cost for tuple position) for each access
- 10-1000 times more expensive than sequential acc.



Family of Threshold Algorithms

- State-of-the-art algorithm for top-k processing
- Independently developed by different groups:
 - Fagin et al. [Fagin03]
 - Güntzer et al. [Güntzer01]
 - Nepal et al. [Nepal99]



Sorted-Access-Only (NRA) Baseline

- Interleaved scans of index lists (round-robin)
- Maintain current high score bound *high_i* for list *i*
- Maintain, for each seen item d:
 - dimensions *E(d)* where *d* has been seen
 - worstscore(d), bestscore(d): score bounds for d Updated whenever d is seen or $high_i$ changes, $i \notin E(d)$
- k items with best worstscores are current top-k; smallest worstscore in top-k: mink
- Prune item d whenever

$$\sum_{i \in E(d)} s_i(d) + \sum_{i \notin E(d)} high_i \le \min k$$

Stop when no candidates ^{i∈E(d)} ^{i∉E(d)}
 left and ∑high_i≤mink ("virtual document check")

CLUSTER OF EXCELLENCE

[Fagin et al., JCSS 03], [Güntzer et al., ITCC 01], [Nepal et al., ICDE 99]

















?

1.0





No more new candidates considered







Background: TREC Benchmark Collection

- TREC Terabyte collection: ~24 million docs from .gov domain, ~420GB (unpacked) size
- 200 keyword topics from TREC Terabyte 2004/5
- Quality measures:
 - Precision at several cutoffs
 - Mean average precision (MAP)
- Performance measures:
 - Number of (sequential, random) accesses
 - Weighted cost C(factor) = #SA + factor · #RA
 - Wall-clock answer time





Experiments: NRA





Improving Sorted Access

- Reduce overhead:
 - Prune candidates not after every step, but after a batch of steps (100-10000)
- Improve List Structure
- Improve List Selection


Inverted block-index



CLUSTER OF EXCELLENCE







- We assign benefits to every block of each list
- Optimization problem
 - Goal: choose a total of 3 blocks from any of the lists such that the total benefit is maximized
 - This problem is NP-Hard, the well known
 Knapsack problem reduces to it
 - But, since the number of blocks to choose and number of lists to choose from are very small, we can solve it exactly by enumerating all possibilities
 - We choose the schedule with maximum benefit, and continue to next round





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Knapsack for Score Reduction (KSR)

• Pre-compute score reduction Δ_{ij} of every block of each list : (max-score of the block – minscore of the block)





Knapsack for Score Reduction (KSR)

- Pre-compute score reduction Δ_{ij} of every block of each list : (max-score of the block – minscore of the block)
- Candidate item d is already seen in list 3. If we scan list 3 further, score s_d and best-score b_d of d do not change
- In list 2, d is not yet seen. If we scan one block from list 2
 - with high probability d will not be not found in that block: best-score b_d of d decreases by Δ_{22}
- Benefit of block B in list i

 $\sum_{d} \Delta_{B} (1 - \Pr[d \text{ found in } B]) \gg \sum_{d} \Delta_{B}$ sum taken over all candidates d not yet seen in list



Knapsack for Benefit Aggregation (KBA)

- Pre-compute expected score e_{ij} of an item seen in block j of list i : (average score of the block)
- Pre-compute score reduction ∆_{ij} of every block of each list : (max-score of the block – min-score of the block)



Knapsack for Benefit Aggregation (KBA)

- Pre-compute expected score e_{ij} of an item seen in block j of list i : (average score of the block)
- Pre-compute score reduction Δ_{ij} of every block of each list : (max-score of the block min-score of the block)
- Candidate item d is already seen in list 3. If we scan list 3 further, score s_d and best-score b_d of d do not change
- In list 2, d is not yet seen. If we scan one block from list
 2
 - either d is found in that block: score s_d of d increases, expected increase = e_{22}
 - or d is not found in that block: best-score ${\rm b_d}$ of d decreases by $\Delta_{\rm 22}$
- Benefit of block B in list i

 $\sum_{d} e_{B} \Pr[d \text{ found in } B] + \Delta_{B} (1 - \Pr[d \text{ found in } B])$ The sum is taken over all candidates d not yet seen in list i





Random Accesses

Two main purposes for random accesses:

- Can speed up execution
- Some predicates cannot be read from sorted lists ("X and not Y") => expensive predicates

Scheduling problem:

• When perform RA for which item to which list?



Random Access Scheduling – When

- Immediately when an item is seen (TA)
 - Scores always correct
 - No need for score bounds & candidates
 - Most RA are wasted (items seen again later)
 - Really slow if RA are expensive
- Balanced: after C sorted accesses, do 1 RA (Combined Algorithm, CA)
 - Faster than TA
 - Most RA are still wasted



Random Access Scheduling – When

• LAST heuristics: switch from SA to RA when

- All possible candidates have been seen
- expected future cost for RA is below the cost already spent for SA
 - Cost spent for SA: known by bookkeeping
 - (simplified) cost expected for RA:



Rationale behind this: Do expensive RA as late as possible to avoid wasting them



Experiments: TREC

TREC Terabyte benchmark collection

- over 25 million documents, 426 GB raw data
- 50 queries from TREC 2005 adhoc task





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Rationale for Approximation Algorithms

- Scoring functions are (well-founded) heuristics, not the gold standard
- Users don't care about the exact top-k results, but about relevant results
- Many relevant results beyond the top-k
- Often one relevant result is enough

Threshold algorithms may be overly conservative



Evolution of a Candidate's Score

TA family of algorithms based on invariant (with sum as aggr) $\sum_{i \in E(d)} s_i(d) \leq s(d) \leq \sum_{i \in E(d)} s_i(d) + \sum_{i \notin E(d)} high_i$

worstscore(d)

bestscore(d)

- Worst- and best-scores
 slowly converge to final
 score
- Add d to top-k result, if worstscore(d) > min-k
- Drop *d* only if

bestscore(d) < min-k, otherwise keep it in candidate queue

 Overly conservative threshold & long sequential index scans

Approximate top-k

"What is the **probability** that *d* qualifies for the top-k ?"





Probabilistic Guarantees

TA family of algorithms based on invariant (with sum as aggr)

$$\sum_{i \in E(d)} s_i(d) \le s(d) \le \sum_{i \in E(d)} s_i(d) + \sum_{i \notin E(d)} high_i$$

Relaxed into probabilistic invariant

$$p(d) := P[s(d) > \delta] = P[\sum_{i \in E(d)} s_i(d) + \sum_{i \notin E(d)} S_i > threshold]$$

$$= P[\sum_{i \notin E(d)} S_i > threshold - \sum_{i \in E(d)} s_i(d)] =: P[\sum_{i \notin E(d)} S_i > \delta'] \leq \varepsilon$$

where the random variable S_i has some (postulated and/or estimated) distribution in the interval (0, high_i]



- Discard candidates with $p(d) \le \varepsilon$
- Exit index scan when candidate list empty





fitting *Poisson* distribution (or Poisson mixture)

- over equidistant values:
- easy and exact convolution
- distribution approximated by *histograms:*
 - precomputed for each dimension

engineering-wise histograms work best!

 $P[d = v_j] = e^{-\alpha_i} \frac{\alpha_i^{j-1}}{(i-1)!}$

dynamic convolution at query-execution time

with independent Si's or with correlated Si's

Probabilistic Guarantees: E[relative precision @ k] = $1-\varepsilon$ E[relative recall @ k] = $1-\varepsilon$



Results for .Gov Queries

on .GOV corpus from TREC-12 Web track: 1.25 Mio. docs (html, pdf, etc.)

50 keyword queries, e.g.:

- "Lewis Clark expedition",
- *"juvenile delinquency",*
- "legalization Marihuana",
- "air bag safety reducing injuries death facts"

	NRA	Prob-Top-k
#sorted accesses	2,263,652	527,980
elapsed time [s]	148.7	15.9
max queue size	10849	400
relative recall	1	0.69
rank distance	0	39.5
score error	0	0.031



.Gov Expanded Queries

on .GOV corpus with query expansion based on WordNet synonyms: 50 keyword queries, e.g.:

- *"*juvenile delinquency *youth minor crime law jurisdiction offense prevention",*
- "legalization marijuana cannabis drug soft leaves plant smoked chewed euphoric abuse substance possession control pot grass dope weed smoke"

	NRA	Prob-Top-k
#sorted accesses	22,403,490	18,287,636
elapsed time [s]	7908	1066
max queue size	70896	400
relative recall	1	0.88
rank distance	0	14.5
score error	0	0.035



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Including Term Expansion

Problem: Users use different terms for similar things \Rightarrow poor recall (missing relevant results)

Example: MPI, MPII, MPI-INF, MPI-CS, Max-Planck-Institut, D5, AG5, DB&IS, MMCI, UdS, Saarland University, ...

Solution:

- 1. Define notion of **similar terms**
- 2. Expand queries with similar terms
- 3. Modify scoring function for expanded queries



[Theobald et al., SIGIR 05]

Heuristics for finding similar terms

Co-Occurrence heuristics:

Terms t₁ and t₂ *similar* if they occur (almost) always together

 $sim(t_{1}, t_{2}) = \frac{2 \cdot |docs(t_{1}) \cap docs(t_{2})|}{|docs(t_{1})| + |docs(t_{2})|}$

Specialization heuristics:

Term t_2 specialization of t_1 if t_1 occurs (almost) whenever t_2 occurs

$$sim(t_1, t_2) = P[t_1 | t_2] = \frac{|docs(t_1) \cap docs(t_2)|}{|docs(t_2)|}$$





Scoring Expanded Queries

Naive approach:

For query term t, add similar terms t' with sim(t,t')> δ to query

But:

"transport

Result quality drops due to topic drift

Better: auto-tuning incremental expansion [SIGIR'05]

For query term t, consider only expansion with

highest combined score per item

$$\overline{s}_t(i) = \max_{t' \in T} sim(t,t') \cdot s_{t'}(i)$$



ane

Incremental Query Expansion

Consider expandable content condition **Professor** with score $\max_{t \in T} \{ sim(Professor,t) * s_t(i) \}$

Dynamic query expansion with incremental, on-demand merging of additional index lists



+ much more efficient than threshold-based expansion
+ no threshold tuning
+ better recall, no topic drift



Effectiveness of Incremental Expansion Approximation



Figure 5: Precision as a function of ϵ - incremental merge vs. static expansion



Efficiency of Incremental Expansion



Figure 8: Efficiency as a function of θ



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Motivation for Text Proximity Scoring

"Bag of words" without term proximity sometimes yields unsatisfactory results

Example: query: Chilean pianists



All query terms individually important, but appear in different paragraphs.

Phrase queries can avoid such bad results. But: prevent also many potentially good results.

[Schenkel et al., SPIRE 07], [Broschart et al., Grundlagen von Datenbanken 08]



Motivation for Text Proximity Scoring



Idea of proximity scores:

Reward occurrences of different query terms in close proximity



What is the best proximity score?



🗖 BM25 📕 ES 📕 Büttcher 🔳 Rasolofo 🔳 Tao,Zhai 📕 Song 🔲 De Kretser,Moffat 📕 LM 🔲 Zhao,Yun 🔳 Lv,Zhai 🔲 Cummins,O'Riordan



[PhD thesis Andreas Broschart – defense next week]





Example: Computation of acc





That's great, but...

Experiments on TREC collection:

approach	P@10	MAP@1000	P@10 stemmed	MAP@1000 stemmed
Büttcher	0.567	0.194183	0.602	0.232466
BM25	0.532	0.184334	0.568	0.215673

Implementation of this score in a top-k-style engine with precomputed inverted lists?



Towards an efficient implementation

Problem: acc(d,t) based on adjacent query terms

 $acc(d,t) = \sum_{t' \in q} \frac{idf(t')}{(pos(t') - pos(t))^2}; t'$ adjacent query term $\neq t$ in d

But: queries not known at index build time

=> we need a query-independent index!

Solution:

$$acc'(d,t) = \sum_{t' \in q} idf(t') \underbrace{\frac{1}{(pos(t') - pos(t))^2}}_{acc(d,t,t')}; t' \text{ every query term} \neq t \text{ in } d$$

Build inverted list with acc(d, t, t') for all term pairs

Document length (in K) does not fit in this framework => drop document length (set b=0)


Index Structures and Results



d: $score_{BM25}(d,t)$

 $d: acd: (acc(d, t_i, t_j), score_{BM25}(d, t_i), score_{BM25}(d, t_j))$

			k=10		k=50		k=100	
	Run	P@k	t[ms]	P@k	t[ms]	P@k	t[ms]	
X	TL	0,57	5.220	0,45	6.868	0,38	8.827	
do'	TL+PXL	0,61	6.266	0,48	11.127	0,40	15.524	
	TL+KL	0,61	821	0,48	1.651	0,40	2.042	



What about the index size?

Construction of query-independent index failed (too slow!)* randomly sampled 1,500,000 term pairs:

1.2% nonempty proximity lists

index/limit	unpruned size(#tuples)	required space
TL	3.191·10 ⁹	47.5 GB
PXL/CL (estimated!)	$1.410 \cdot 10^{12}$	20.5 TB / 41.0 TB

keeping all proximity lists: infeasible

Pruning might be the solution:



horizontal pruning and hertizental upringing



*we fixed that now

Different horizontal pruning methods

- limit distance of term occurrences
- limit proximity score
- limit list size to a constant (from 500 to 3,000 tuples)
- Carmel et al. [SIGIR 2001]: static index pruning drop index entries having scores below ε·top-k score
- combinations (e.g., limit list size + static index pruning)



Horizontal pruning helps a lot

Index size: in million tuples (estimated)

index/limit	500	1000	1500	2000	2500	3000	unpruned
TL	295	355	402	442	472	496	3,191
PXL/CL (est.)	368,761	435,326	481,949	515,079	542,611	566,277	1,410,238
PXL/CL, score \geq 0.01 (est.)	23,050	28,855	34,023	38,985	42,085	45,186	87,049

Index size: in bytes (estimated)

index/limit	500	unpruned
PXL (est.)	5.4 TB	20.5 TB
CL (est.)	10.7 TB	41.0 TB
PXL, score \geq 0.01 (est.)	343.5 GB	1.3 TB
CL, score \geq 0.01 (est.)	686.9 GB	2.5 TB

Index size of (real) file-based index

Index/max. Länge	3.000	ungekürzt
TL	2,9 GB	34 GB
$PXL(window \leq 5)$	133 GB	311 GB
KL(window≤5)	266 GB	622 GB



Top-10 retrieval: unpruned vs. pruned lists

Configuration	P@10	Cost(1000)	index size(est.)
BM25(=TL)	0.56	1,956,193,840	47.5 GB
TL(2000 tuples)	0.34	9,303,808	6.6 GB
TL+CL	0.60	187,999,568	41.0 TB
TL+CL(2000 tuples)	0.60	25,971,904	15.0 TB
$TL+CL(\epsilon=0.025)$	0.60	73,744,304	
$TL+CL(\epsilon=0.1)$	0.60	84,484,976	n/a
$TL+CL(\epsilon=0.2)$	0.58	105,584,992	
$TL+CL(500; \epsilon=0.025)$	0.54	6,628,528	n/a
$TL+CL(2000; \epsilon=0.025)$	0.60	20,377,904	
$TL+CL(500; score \ge 0.01)$	0.58	6,931,904	691.3 GB
$TL+CL(1000; score \geq 0.01)$	0.60	12,763,376	865.3 GB
$TL+CL(1500; score \geq 0.01)$	0.61	18,117,552	1.0 TB
TL+CL(2000; score≥0.01)	0.61	22,734,544	1.1 TB



Query Processing with Merge Joins



prune and resort index lists



Evaluation



Static index pruning for TL+CL

Our pruning approach

- keep all pair lists (more precise: CLs)
- tune list length l and
- minimum acc_d -score m and text window size W=10 for CLs



- Apply compression to docid-ordered index lists:
 - docid values: delta-encoding + v-byte encoding
 - scores: v-byte encoding (normalization $\Rightarrow \leq$ 2bytes each)

I(C, l, m): index for collection C with TLs and CLs cut after l entries and only keeping CL tuples with $acc_d \ge m$ (and text window W=10)



Index tuning

Two optimization goals:

- effectiveness-oriented index tuning: best retrieval quality within index size constraint (then minimize size)
- efficiency-oriented index tuning: at least BM25 quality and query processing as fast as possible.

Available input data:

- absolute index quality tuning: we have relevance assessments
- relative index quality tuning: we do not have relevance assessments





[Broschart2012]

Index quality measures

Goal: choose pruning parameters l and m for a given collection C, an upper limit S for the index size, and a result cardinality k s.t. the index quality measure M(C, l, m, k) is maximized.

Absolute index quality tuning:

input: training topics Λ + their **relevance assessments** $p_{\Lambda}[k; I]$: average quality of top-*k* results (e.g., P@*k*) over Λ on index *I*

effectiveness-oriented: maximize $M(C, l, m, k) = p_{\Lambda}[k; I(C, l, m)]$

```
Example (S = 150GB, k = 10)
```



	index	l	m	size(index)	$p_{\Lambda}[k;index]$
	I_1	210	0.1	110GB	0.50
	I_2	310	0.1	120GB	0.51
IS	I_3	410	0.15	130GB	0.51
	I_4	510	0.1	140GB	0.52
	I_5	610	0.1	150GB	0.52

Maximize precision for all feasible indexes: equally high precision of I_4 and I_5 Pick index with smaller index size I_4



Index quality measures

Goal: choose pruning parameters l and m for a given collection C, an upper limit S for the index size, and a result cardinality k s.t. the index quality measure M(C, l, m, k) is maximized.

Absolute index quality tuning:

input: training topics Λ + their **relevance assessments** $p_{\Lambda}[k; I]$: average quality of top-*k* results (e.g., P@*k*) over Λ on index I

efficiency-oriented: maximize $M(C, l, m, k) = \begin{cases} \frac{1}{l} & \text{if } \frac{p_{\Lambda}[k; I(C, l, m)]}{p_{\Lambda}[k; T(C)]} \ge 1\\ 0 & \text{else} \end{cases}$

Example (
$$S = 150GB, k = 10$$
)

 l_5

 $\forall I_x : size(I_x) < \overline{S}$

Λ

$$p_{\Lambda}[k;T(C)] = 0.51$$

index	l	m	size(index)	$p_{\Lambda}[k;index]$
I_1	210	0.1	110GB	0.50
I_2	310	0.1	120GB	0.51
I_3	410	0.15	130GB	0.51
I_4	510	0.1	140GB	0.52
I_5	610	0.1	150GB	0.52

Candidates = $\{I_x : \frac{p_{\Lambda}[k;I_x]}{p_{\Lambda}[k;T(C)]} \ge 1\}$ Lowest length for I_2 = maximal index [

Warm cache comparison to BMW

50,000 queries from TREC Terabyte Efficiency Track 2005:

compare fastest index (I,m)= (310,0.05) (efficiency-oriented index tuning) to state-of the art DAAT-algorithm BMW. Use LRU cache of varying size.

		cache	cache hit ratio		#non-cached	
\overline{l}	\overline{m}	size[MB]	[bytes]	[#lists]	lists	$\varnothing t_{warm} \; [ms]$
310	0.05	8	28.98%	29.29%	161,393	39.85
310	0.05	16	37.05%	37.08%	143,613	36.04
310	0.05	32	44.36%	43.89%	128,069	32.70
310	0.05	64	50.54%	49.39%	$115,\!525$	29.67
310	0.05	1024	54.44%	52.77%	107,801	28.92

		cache	cache h	it ratio	#non-cached		
k	index	size[MB]	[bytes]	[#lists]	lists	#read blocks	$\emptyset t_{warm}$ [ms]
10	$T(C)_{BMW}$	64	3.62%	2.15%	$115,\!938$	$397,\!735,\!689$	204.63
100	$T(C)_{BMW}$	64	3.62%	2.15%	$115,\!938$	573,001,133	259.01
10	$T(C)_{BMW}$	1024	46.39%	26.58%	86,990	397,735,689	173.16
10	$I'(C)_{BMW}$	1024	44.02%	14.57%	$197,\!638$	$312,\!500,\!850$	206.36

Speedup of our approach: factor 7 for top-10, factor 9 for top-100 retrieval (cache hit ratio 50% vs less than 4%) Index size: (310,0.05): 94.9GB, $T(C)_{BMW}$: 10.5GB, $I'(C)_{BMW}$: 221.0GB



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 - Top-k with Constrained Budget
- Efficient Precomputation
- Efficient Distributed Query Processing



Dual Optimization Problem

So far:

Minimize answer time for optimal results But: this may take too long (several seconds).

Now:

Maximize result quality for given answer time (or processing cost)

User-oriented efficiency measure



[Shmueli-Scheuer et al., ICDE 09]

Classes of Top-k Algorithms

- Budget-Keeping Algorithms: Execution cost never exceeds predefined limit
- Budget-Oblivious Algorithms: Scheduler does not know cost limit (Anytime-algorithms)
- Budget-Aware Algorithms:

Scheduler knows cost limit in advance, optimizes for result quality when limit is hit



Measuring Result Quality

Gold standard:

Results R_{opt} of top-k algorithm with unlimited budget

Goal:

Optimize relative overlap of results R with R_{opt}



Traces for a query

Trace: sequence of steps performed by an algorithm

- Sequential scan in a list (cost 1)
- Random access to a previously read item (cost C)

Cost of a trace: sum of cost of its steps

Results of a trace: Results of a top-k algorithm performing the steps of the trace in this order



Optimization problem

Given a query with the corresponding lists, find a trace with cost ≤ B with a result that maximizes relative overlap with R_{opt}



This is a nontrivial problem.

	L_1	L_2
1	s:0.95	a:1.00
2	u:0.93	b:0.90
3	t:0.92	c:0.85
4	d:0.90	d:0.80
5	x:0.50	t:0.60
6	y:0.40	e:0.40
		.
7		

Fig. 2. Prefixes of two lists

C=3 (cost for random access)

Final top-2 result: {d,t}

Correct result requires at least budget 9 (4SA in L1, then 2RA to L2 for d and t)

For precision 0.5, we need at least budget 6 (t)

TA: budget 12 to find {t}, budget 16 to find {d,t}

NRA with round-robin: 8 steps to find {d}, 10 steps for {d,t}

Results depend on clever scheduling of SA and RA



Heuristics for SA scheduling 1

Two execution phases (without sharp transition):

- Gathering: Find good candidate items (with high scores) that may be in final top-k
- Reducing: Decide for k results in the final top-k (reducing score bounds by dropping list high score bounds)

Rule of thumb: Mediocre scores don't help





Heuristics for SA Scheduling 2

Schedule batches of size *b* (*b*<
budget)
Utility functions for performing *x* scans on list *i*:

• Based on average score

$$util_{as}(L_i, x) = \frac{1}{x} \cdot \sum_{j=pos_i}^{pos_i + x} score_i(j).$$
(1)

• Based on score drop

$$util_{sr}(L_i, x) = high_i - score_i(pos_i + x).$$
(2)



Heuristics for SA Scheduling 3

Combined utility for optimization: $util(L_i, x) = \alpha \cdot util_{as}(L_i, x) + (1 - \alpha) \cdot util_{sr}(L_i, x).$ (3)

where α depends on the phase:





Heuristics for SA Scheduling 4

Fair scheduling of the next b accesses:

Assign to each list L_i a number SA_{Li} of SA

$$SA_{L_i} = b \times \frac{util(L_i, b)}{\sum_{j=1}^m util(L_i, b)}$$
(6)

More complex (and more effective) heuristics



Experiments: SA Scheduling



Fig. 6. TREC: average percentage of optimal precision, k=100, varying budgets



RA Scheduling is a Lot More Difficult

Key questions to answer:

- When to switch from SA to RA?
 - Need to have seen "enough" items
 - Need to have "enough" budget left
- Which items to access?
 - Goal: RA only for "good" items, not to eliminate candidates

Some results, but far from real understanding



Part 1 – Uncovered Issues

- Inverted file organization, compression, ...
- Caching of (partial) results
- Hardware issues
 - Multicore CPUs
 - Memory hierarchies (CPU caches, flash disks)
 - Nonstandard hardware (FPGA, GPU)
- Parallel and Distributed Retrieval
 - Distribute & replicate lists over different machines
 - Query distributed data over the Web
- XML retrieval



Part 1 – Summary

- Top-k processing central part of search engines
- Basic problem well understood in the literature
- Good engineering can make the difference

- Many interesting problems still out there
 - Heuristics are good, but guarantees would be better.



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- Efficient Distributed Query Processing



Web-Scale Computation

Many problems cannot be easily scaled to the Web

(about 20TB per Google crawl)

(commoncrawl.org: 5 billion pages, 60TB)

- Document inversion
- PageRank etc. computation
- Web log mining
- Host statistics
 - Term distribution per host
 - Accesses per host



Motivation





Large Clusters of Commodity Hardware

- Thousands of off-the-shelf networked PCs
- Hardware failures (of single machines) common
- Harddrive failures common

• Distributed Programs to exploit full power (RPC, CORBA, MPI, WebServices, REST, ...?)



MapReduce Features

- Complete solution for distributed computing
- Simple, but powerful interface
- Implementation within hours, not weeks
- **Detects** machine failures and **redistributes** work
- Avoids data loss due to harddisk failures (together with distributed file system)

Widely used at Google for daily business (2 mio MapReduce jobs in Sep 07 on 15TB each, 400s each)



[Dean et al., CACM 51(1), 2008]

MapReduce by Example

Problem: Compute document frequencies

- Input: data with keys (docs with docids/urls)
- Output: aggregated data (terms with counts)

Solved by two functions (provided by user):

- MAP: partition input data by output key (term)
- **REDUCE**: aggregate data for each output key

Automatically executed in a distributed fashion



MapReduce by Example

```
map(String key, String value)
  // key: document name
  // value: document content
  for each term in value:
    EmitIntermediate(term,1);
reduce(String key, Iterator values)
  // key: term
  // values: list of counts
  int result=0;
  for each v in values:
    result:=result+value;
  Emit(term, result);
```



Architecture



taken from [Dean et al., CACM 51(1), 2008]

Architecture

- Dedicated master process identifies worker processes/machines for map and reduce
- Master **partitions** input file into M partitions
- Partitions assigned to map workers
- Map workers output to R files on local hard disks (by hash code), master notified
- Each reduce worker reads one output file from the map workers (by RPC) & sorts them (many output keys per file!)
- Each reduce worker aggregates data per key


Failure Handling

- Master monitors workers
- On worker failure:
 - All MAP tasks marked failed and submitted to other workers (including finished ones – data on local hard disk!)
 - All active REDUCE tasks resubmitted to other workers
 - Requires idempotence of operations (workers could just be slow, not failed)



Application Example: PageRank

• Definition of PageRank

$$PR(v) = \varepsilon \sum_{(u,v)\in E} \frac{PR(u)}{\text{outdeg}(u)} + (1 - \varepsilon)$$

- Computed through power iteration: values in step i computed from values in step i-1 and graph structure
- Highly local computation: requires only old pageranks from incident nodes



PageRank in MapReduce







[Picture probably courtesy of Jimmy Lin or Christophe Bisciglia et al.]

Initial Step

MAP: (url, content) (url, (initial pagerank, list(linked urls)))

REDUCE:

Passes input tuples to output without change



Iteration Steps

MAP: (url, (PR, list(n linked urls))) (linked url 1, PR/n), ..., (linked url n, PR/n), (url, list(n linked urls) **REDUCE:** (url, PR1),...,(url, PRx), (url, list(linked urls)) (url, (PR', list(linked urls)))



Termination

Terminate when values are stable (determined by central component)



Implementations freely available

 PIG (Yahoo) <u>http://research.yahoo.com/node/90</u>

- Hadoop (Apache) <u>http://hadoop.apache.org/</u>
- DryadLinq (Microsoft) <u>http://research.microsoft.com/research/sv/DryadLINQ/</u>



Pig Latin vs. SQL

SELECT category, AVG(pagerank)
FROM urls WHERE pagerank > 0.2
GROUP BY category HAVING COUNT(*) > 10⁶

```
good_urls = FILTER urls BY pagerank > 0.2;
groups = GROUP good_urls BY category;
big_groups = FILTER groups BY COUNT(good_urls)>10<sup>6</sup>;
output = FOREACH big_groups GENERATE
category, AVG(good urls.pagerank);
```



Part 2 – Summary

- MapReduce is a powerful framework for distributed computing
- Exploits potential of commodity hardware

• Hadoopify your applications!

• But: Does not solve everything



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 - Document-based partitions



Simplified Preprocessing Procedure

 For each document d in the collection for each term t contained in d emit tuple (t,d,score(d,t)) to temp storage

- 2. Group tuples by term
- 3. Build inverted lists for Cache Cartering

Reduce phase of a MapReduce job

Natural steps to exploit distribution: 1+3

- Assign subcollections to different machines and parse documents at these machines
- Iwo alternatives:
 - Generate local index for each subcollection
 - Combine all temp data, partition it by term to different machines, create global inverted list for each term



Two distribution models

Index can be distributed in two ways:

- Partitioned by terms (complete index lists at different machines);
 often the outcome of index creation
- Partitioned by documents (subcollections with their own indexes at different machines);
 often caused by natural distribution of data
- Result of horizontal partitioning of table, can be seen as "distributed database" with one logical table:



D1	t1 t2	d1 d1	score(d1,t1) score(d1.t2)
or			
	t1	d2	score(d2,t1)
D2	t2	d2	score(d2,t2)
	t1	d3	score(d3,t1)



QP for Term-Based Partitions

Can we apply straight-forward techniques from distributed databases?

Assume query with 3 terms at 3 (different) nodes, compute top-1

- Ship all to one node (here, the query initiator Q)
- (Semi-)Join at Q, sum scores, project terms away, sort by score



d5 0.7

cost: 3 messages, 20 attribute values





Basic distributed top-k algorithm: TPUT Assume query with m terms at m (different) nodes Three phases, driven by query initiator Q:

- Collect top-k entries from all lists at Q, join and sort them by score, denote score of current top-k by mink
- Collect all entries with score at least mink/m from all lists at Q, recompute current top-k and mink, prune candidates
- 3. Get missing scores for all remaining candidates

(Easy) Theorem:

Step 2 does not miss any final top-k results, TPUT is correct.



TPUT for the example

- Each node ships top-1 local entry to Q
- (Semi-)Join at Q, sum scores, project terms away, sort by score
- Each node ships entries with score ≥mink/3 to Q
- Update scores at Q
- Get missing scores for remaining candidates, update scores





Improvements for TPUT

- Locality: Execute query at node with longest list, send only result to Q
- Approximation: Drop last phase, drop some lists (but: which lists?)
- Hierarchically group operators
- Distribute mink threshold not uniformly, but in a way that minimizes (estimated) number of
 in a
 in a



CLUSTER OF EXCELLENCE

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2 important use cases for doc-based p.

Distributed indexing (always "cooperative")

- scale out indexing by distributing existing collection over many nodes
- Keep index at each node (plus optional extra nodes)
- ⇒ scale out query processing as well (indexes in memory)

• Federation of independent search engines

- Document partitions built independently (crawlers, digital libraries, archives)
- Local indexes built independently
- Perform federated queries over all search engines (examples: excite.com, metager.de)



2 important use cases for doc-based p.

Distributed indexing (always "cooperative")

- scale out indexing by distributing existing collection over many nodes
- Keep index at each node (plus optional extra nodes)
- ⇒ scale out query processing as well (indexes in memory)
- Federation of independent search engines

Important distinction:

• cooperative sources provide details about scores (implementations, parameters, statistics, ...) and allow partial access to their collection (e.g., for computing new statistics)

 uncooperative sources provide only a query-based interface and no access to internal operations (only sampling possible)



QP for doc-based partitions

- Documents distributed over multiple servers (may or may not include duplicates)
- Straight-forward top-k query processing:
 - Submit top-k query to all servers
 - Collect results at dedicated machine & combine to overall top-k



Correctness under score equivalence

Correctness:

combination of local top-k results identical to top-k result in unpartitioned collection

- straight-forward for **partitioned database**
- Not necessarily true for **distributed search engine**:
 - Indexes may be build locally
 - Scores may be computed locally (with local document frequencies!)
- Solution: Make sure that local and global scores are equivalent (e.g., keep global document freq.)
- Additional complication: Local optimizations (pruning of entries with low scores, ...)



What if score equivalence is impossible?

- Scores may be **incomparable** (different scoring models or even **no scores** at all, e.g., Google)
- **Result Merging** (or Fusion) in such settings:
 - Round Robin:
 - Order sources by expected usefulness S_i (see later)
 - Pick result 1 from source 1, result 1 from source 2, etc.
 - Use source-normalized scores:
 - Normalize scores for all docs from a source to [1.0;0.0]
 - Multiply scores by expected usefulness to get sourced-normalized scores
 - Rank documents in order of sourced-normalized score
 - Use machine learning to predict scores:
 - Collect samples of each collection in central place
 - Learn correllation of result scores on centralized sample and in each collection (from large training set of queries)

Improving Efficiency: Two Paths

- Reduce number of results per partition
 - For global top-k, usually local top-k' sufficient (with k'<<k)
 - But: safe choice of local k' difficult (depends on scores of local results), estimation based on local score distribution (done at central node!)
 - Approximate, not exact query results
- Reduce number of partitions accessed
 - Many partitions have no (or hardly any) good results (esp. in federations over multiple domains)
 - Preselect a few good partitions for querying based on expected usefulness ("collection selection problem")
 - Approximate, not exact results





df_i(t): number of documents in db_i that contain term t
cw_i(t): number of words in db_i
avg(cw): average number of words in collections
|DB|: number of collections
cf(t): number of collections that contain term t

Given query Q={t1,...,tn}, rank sources by average belief

[Callan et al., 1995]



Extensions for Collection Selection

- Consider size of collection: larger collection should give more "good" results [Si, 2006]
- Consider overlap of collections: if two collections are largely overlapping, consider only one of them ("diversity" of collections) [Bender et al., 2005]
- Estimate usefulness of collection from sample: Estimate number of relevant results from subcollection from scores of docs in sample (e.g., ratio of documents in sample with score>threshold, divided by sample ratio) [Si&Callan, 2003]



Upwards Down: Document Allocation

- Goal: Create partitions such that "usually" a small number of collections is sufficient per query
- Options for document allocation:
 - Randomized
 - Group documents per source (e.g., Web server)
 - Group documents per topic:
 - Build coherent clusters of subset of documents
 - Assign remaining docs to clusters
 - Each cluster forms a partition



Example for Document Allocation

- TREC ClueWeb09-CatA collection (~500M docs)
- 50 standard benchmark queries
- Sample size 1%, 1000 partitions



Figure 3: Distribution of shard sizes for the topicbased shards of the Clue-CatB dataset.



Figure 6: Distribution of relevant documents across top shards for the three allocation policies for the Clue-CatA-Eng dataset. Total number of relevant documents: 5684

figures from [Kulkarni and Callan, 2010]



Summary: Distributed IR

- Techniques in general very similar to DDBS
- Main techniques:
 - Distributed top-k
 - Collection selection
- Approximative variants very common (unlike in distributed databases, but may have applications there as well)



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